Math 100 - Week 7 Recitation (Fall 2013)

The purpose of this week's activity is to reinforce the difference between sequences and series. For each of the following expressions a_n , your goal is to

- (a) Determine whether the sequence $\{a_n\}$ converges or diverges.
- (b) If the sequence converges, find its **limit**.

(c) Determine whether the series
$$\sum_{n=1}^{\infty} a_n$$
 converges or diverges.

(d) If the series converges, find its **sum**.

At the end of the recitation session, as a sample of your work, each group will be asked to submit solutions (all four parts) to three of the problems on the worksheet; you may choose any three. These problems will be graded to determine recitation grades for all the group's members. Remember, as always, that these solutions should be a consensus, agreed on by all members of your group.

(Note: The square brackets in Problems 4, 5, and 8 are no different from parentheses... they're just there to make some of the complicated formulas more easily readable.)

1.

$$a_{n} = \frac{2^{2n} + 3^{n}}{5^{n-1}}$$
2.

$$a_{n} = \frac{2^{n} + 3^{2n}}{5^{n+1}}$$
3.

$$a_{n} = \frac{4e^{n} + n^{2}}{9e^{n} + 2n}$$
4.

$$a_{n} = [n^{3} + 1]^{-1/3} - [(n+2)^{3} + 1]^{-1/3}$$
5.

$$a_{n} = [n^{3} + 1]^{1/3} - [(n+2)^{3} + 1]^{1/3}$$
6.

$$a_{n} = (2^{n} + 1)e^{-n}$$
7.

$$a_{n} = (4^{n} + 1)\pi^{-n}$$
8.

$$a_{n} = \ln[n(n+2)] - \ln[(n+1)^{2}]$$